

# PHY 207

# Practice Test III

Name: \_\_\_\_\_

Student ID: \_\_\_\_\_

Answer the all four problems. Partial credits are based on the clarity and the quality of the work you show.

$$\vec{E} = \frac{kq}{r^2} \hat{r}, k = \frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ NM}^2\text{C}^{-2}, \vec{F} = q\vec{E}, \oint \vec{E} \cdot d\vec{A} = \frac{Q_{in}}{\epsilon_0},$$

$$V = \frac{kq}{r}, V = \int \frac{k dq}{r}$$

$$dV = \frac{dU}{q} = -\vec{E} \cdot d\vec{l} = -(E_x dx + E_y dy + E_z dz), \vec{E} = -\nabla V = -\left(\frac{\partial V}{\partial x} \hat{i} + \frac{\partial V}{\partial y} \hat{j} + \frac{\partial V}{\partial z} \hat{k}\right),$$

$$V = Ed, C = \frac{Q}{V}, U = \frac{1}{2} \sum q_i V_i, U = \frac{1}{2} CV^2 = \frac{1}{2} \frac{Q^2}{C}, u_e = \frac{1}{2} \epsilon E^2, \epsilon = K\epsilon_0$$

$$V = IR, P = IV = I^2 R, I = \frac{dQ}{dt} = nqvA, J = \frac{I}{A}, E = \rho J, R = \frac{\rho l}{A}, R = R_1 + R_2 + \dots, \frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

$$I = I_0 \exp\left(\frac{-t}{RC}\right), F = qv \times B, dF = Idl \times B, \mu = NIA\hat{n}, \tau = \mu \times B$$

$$B = \frac{\mu_0}{4\pi} \frac{qv \times \hat{r}}{r^2}, dB = \frac{\mu_0}{4\pi} \frac{Idl \times \hat{r}}{r^2}, u_m = \frac{B^2}{2\mu_0}, B = \mu_0 nI$$

$$\oint B \cdot dl = \mu_0 \left(I + \epsilon_0 \frac{d\Phi_E}{dt}\right), \mu_0 = 4\pi \times 10^{-7} \text{ Tm/A},$$

$$\oint E \cdot dl = -\frac{d\Phi_M}{dt}, \Phi_M = \int B \cdot dA, \Phi_M = LI$$

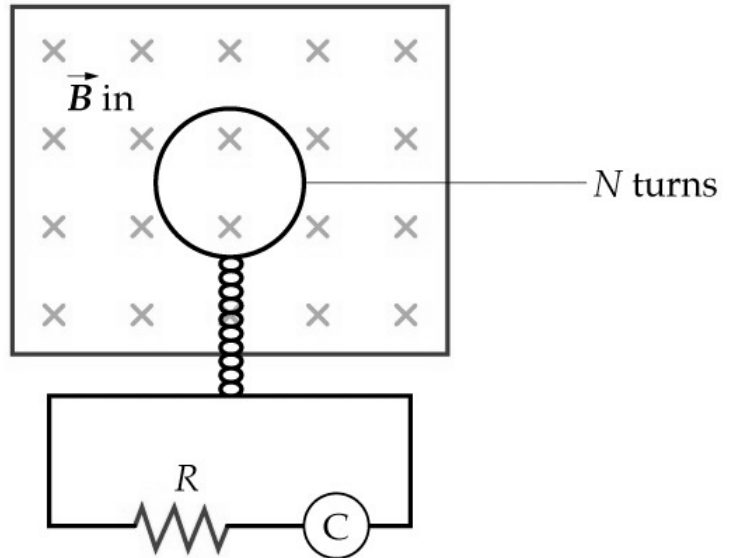
$$\epsilon = Blv, \epsilon = -\frac{d\Phi_M}{dt}, \epsilon = -L \frac{dI}{dt}, I = I_0 \exp\left(\frac{-R}{L}t\right)$$

$$A_{sph} = 4\pi r^2, V_{sph} = \frac{4}{3}\pi r^3, dV_{sph} = 4\pi r^2 dr$$

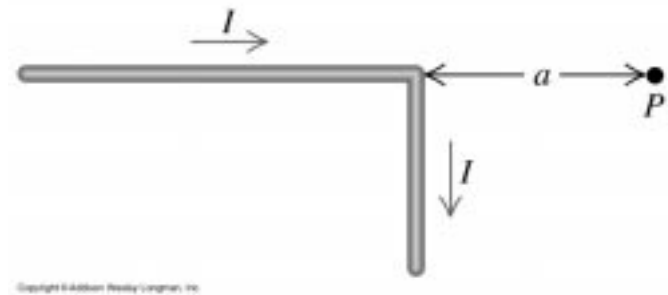
$$A_{cyl} = 2\pi rL, A_{cir} = \pi r^2, dV_{cyl} = 2\pi r dr L$$

$$dq = \lambda dl = \sigma dA = \rho dV$$

A small coil of  $N$  turns has its plane perpendicular to a uniform magnetic field  $B$  as shown. The coil is connected to a current integrator, a device used to measure the total charge passing through it. Find the charge passing through the coil if the coil is rotated through  $180^\circ$  about its diameter.



The wire in the figure is infinitely long and carries a current  $I$ . Calculate the magnitude and the direction of the magnetic field at point  $P$ .



A long, cylindrical wire of radius  $a$  carries current  $I$  uniformly distributed over its cross-sectional area. A) Find the magnetic field everywhere ( $r < a$ , and  $r > a$ ); B) Find the magnetic field energy per unit length within the wire.

A long straight wire carries a constant current  $I$ . A square conducting loop of length  $L$  is moving at a velocity  $\mathbf{V}$ , as shown in the figure. At the instant when the near side of the loop to the wire is  $x$ , find the direction and magnitude of the induced current in the loop. Assume the resistance of the loop is  $R$ .

